1. Let be a discrete random variable, and let and be two disjoint (that is, ) and exhaustive (that is, ) subsets of the sample space . Prove

The law of total expectation states that,

Where are portions of the whole space . Next, we know that and are the partitions that form , therefore,